

MUMAX3-WORKSHOP

SESSION 1

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WORKSHOP SCHEDULE

Monday 08/31, 6PM-8PM CET

Session 1: general introduction to micromagnetics in mumax3

Session 2: mumax3 ecosystem, workflow and a first simulation

Monday 09/07, 6PM-7:30PM CET

Session 3: basic examples

Homework

Monday 09/14, 6PM-7:30PM CET

Session 4: advanced features and more extensive examples

SESSION 1: GENERAL INTRODUCTION

Part 1: Micromagnetics recap

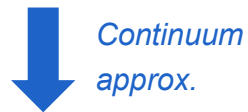
- Magnetization field
- Magnetic energy
- Magnetization dynamics
- Energy minimization

Part 2: Design of mumax3

- Mumax3 in a nutshell
- Scripting language
- Discretization
- Shapes, geometry, regions
- Material parameters
- Initial magnetization
- Output
- Run/Relax/Minimize
- Effective field terms
- Spin transfer torques

MICROMAGNETISM

In ferromagnets, neighboring magnetic moments have the tendency to align



Magnetization can be described by a continuous vector field

$$\mathbf{M}(\mathbf{r}, t) = M_s(\mathbf{r}) \underbrace{\mathbf{m}(\mathbf{r}, t)}_{\text{central quantity of interest}}$$

- picosecond time scale
- 1nm – 1μm length scale



Quasi-uniform state



Vortex



Néel Skyrmion

MICROMAGNETISM

The physics is fully described by the total magnetic energy functional:

$$E[\mathbf{m}] = \int_V \left\{ \begin{array}{l} A(\nabla\mathbf{m})^2 \\ \text{Exchange} \end{array} \right. - \mu_0 \mathbf{M} \cdot \mathbf{H}_{ext} \quad \begin{array}{l} \text{Zeeman} \\ \end{array} - \frac{\mu_0}{2} \mathbf{M} \cdot \mathbf{H}_{demag} \quad \begin{array}{l} \text{Demagnetizing field} \\ \end{array} + \left. \begin{array}{l} \text{Crystal anisotropy} \\ \text{Dzyaloshinskii-Moriya} \\ \text{Magneto-elasticity} \\ \text{Higher-order exchange} \\ \dots \end{array} \right\} d^3\mathbf{r}$$



MICROMAGNETISM

Two main objectives



Time integration *dynamics*

- Spin waves
- Domain wall motion
- Spin transfer torques
- Vortex excitation
-

Energy minimization *statics*

- Stable magnetic states
- Hysteresis curves
- Phase diagrams
- Domain wall profiles
- ...

MICROMAGNETISM

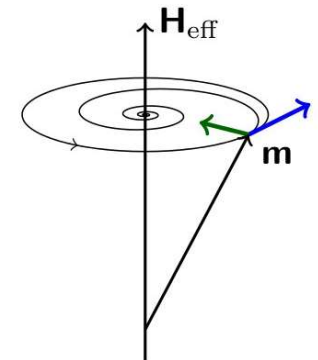
Time integration
dynamics

The magnetization dynamics is described by the Landau-Lifshitz-Gilbert (LLG) equation

$$\dot{\mathbf{m}} = -\frac{\gamma}{1 + \alpha^2} \left[\underbrace{\mathbf{m} \times \mathbf{H}_{eff}}_{\text{precession}} + \alpha \underbrace{\mathbf{m} \times (\mathbf{m} \times \mathbf{H}_{eff})}_{\text{damping}} \right]$$

with

$$\mathbf{H}_{eff} = -\frac{1}{\mu_0 M_s} \frac{\delta E}{\delta \mathbf{m}}$$



Computation of the magnetization dynamics:

$$E[\mathbf{m}, t] \rightarrow H_{eff}(\mathbf{r}) \xrightarrow[\text{LLG}]{\text{LLG}} \mathbf{m}(\mathbf{r}, t)$$

MICROMAGNETISM

Time integration
dynamics

LLG adaptation 1

Spin transfer torques (Zhang-Li^[1], Slonczewski^[2,3])

$$\dot{\mathbf{m}} = -\frac{\gamma}{1 + \alpha^2} [\mathbf{m} \times \mathbf{H}_{eff} + \alpha \mathbf{m} \times (\mathbf{m} \times \mathbf{H}_{eff})] + \tau_{STT}$$

LLG adaptation 2

Additional random effective field term which scales with the temperature^[4]

$$\mathbf{H}_{eff} \rightarrow \mathbf{H}_{eff} + \mathbf{H}_{th}$$

$$\langle \mathbf{H}_{th}(\mathbf{r}, t) \rangle = 0$$

$$\langle \mathbf{H}_{th}(\mathbf{r}, t), \mathbf{H}_{th}(\mathbf{r}', t') \rangle = \frac{2k_B T \alpha}{M_s \gamma} \delta(\mathbf{r} - \mathbf{r}') \delta(t - t')$$

MICROMAGNETISM

Energy minimization
statics

Two approaches to minimize the free energy functional numerically:

1. Standard minimization scheme (*e.g. steepest gradient*)
2. LLG equation with strong damping (*=removing the precession term*)

$$\dot{\mathbf{m}} = -\mathbf{m} \times (\mathbf{m} \times \mathbf{H}_{eff})$$

WHAT IS MUMAX3?

- Free finite-difference based micromagnetic simulation package
- GPU-accelerated *nvidia GPU required*
- Developed at DyNaMat (Ugent) by Arne Vansteenkiste
- Latest official release mumax3.10 (*Aug 13, 2020*)
- Active community groups.google.com/forum/#!forum/mumax2
- Documented API mumax.github.io
- Open source (GPLv3) github.com/mumax/3
- Mainly written in Go
- CUDA C kernels for heavy lifting
- Scripting language + Web GUI
- Well tested (unit tests + NIST standard problems)

Golang



SCRIPTING LANGUAGE

Mumax3's scripting language is a subset of goLang

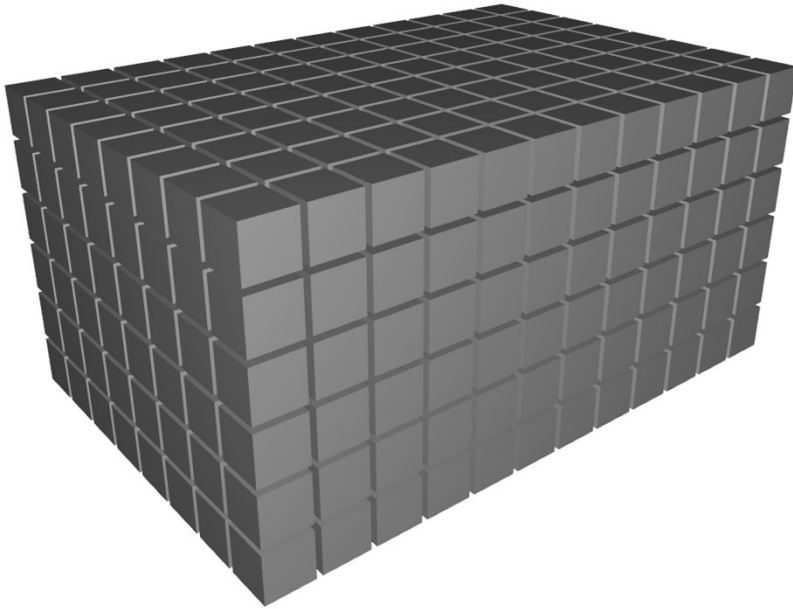
```
// saturation magnetization
Msat = 5e6

// declare new variable
Freq := 1e9

for i:=0; i<10; i++ {
    print(i)
}

if 1+8 == 9 {
    print("Of course 1+8=9")
}
```

DISCRETIZATION



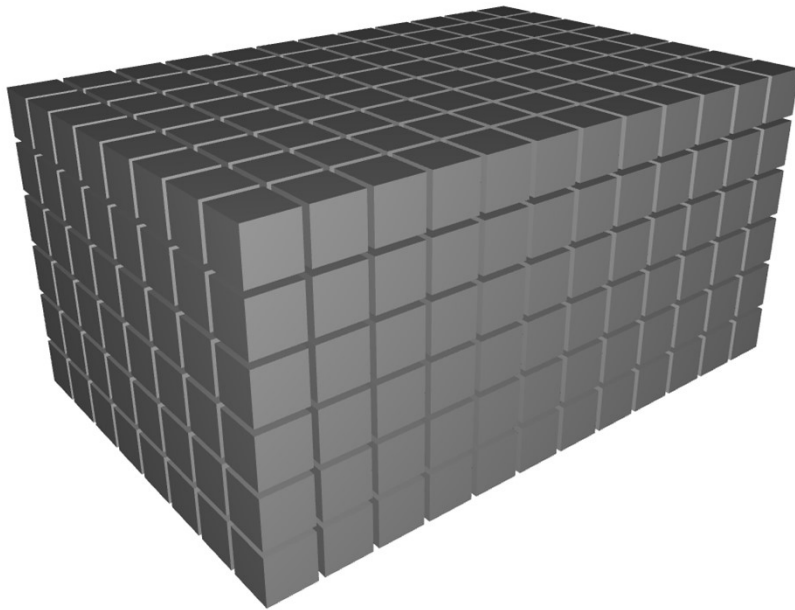
- Rectangular simulation box (origin in the center)
- Single regular rectangular grid
- Uniform magnetization inside cell $\mathbf{m}_{ijk} = \mathbf{m}(x_i, y_j, z_k)$
- Cell size < exchange length

```
setgridsize(256,64,1)  
setcellsize(1e-9,1e-9,1e-9)
```

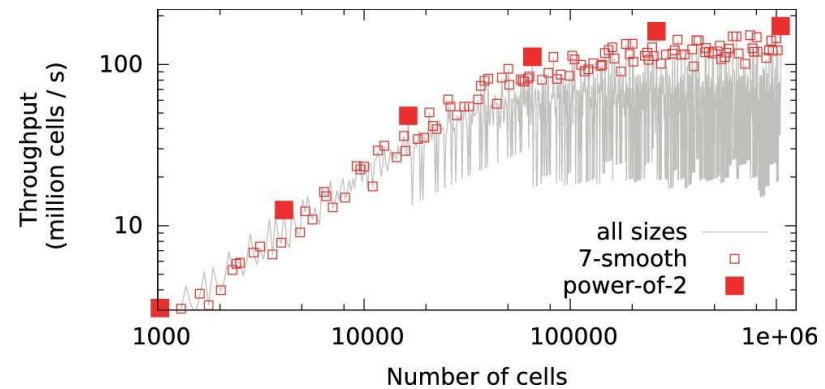
- PBC values are number of virtual repetitions of the simulation box used to calculate dipolar interactions

```
setpbc(4,0,0)
```

DISCRETIZATION



The cuda fft library (used for the computation of the demag field) is highly optimized for grid size dimensions with small prime factors.



Tip: try to use grid size dimensions which are '7-smooth'

Example of good and bad grid size dimensions:

$$190 = 2 \cdot 5 \cdot 19$$



$$191 = 191$$



$$192 = 2^6 \cdot 3$$



SHAPES

- A shape can be considered as a function $f: \mathbb{R}^3 \rightarrow \{true, false\}$ where

$$f(x, y, z) = \begin{cases} true & \text{if } (x, y, z) \text{ in shape} \\ false & \text{otherwise} \end{cases}$$

- Most shapes do not depend on the grid
- Default location: center of universe (0,0,0)
- Large set of predefined basic shapes
- Define new shapes by combining and modifying the basic shapes
- Shapes are useful for different tasks:
 - The geometry
 - Defining regions
 - To set locally an initial magnetization

SHAPES

Shapes

Cell(j,k,l)
Circle(diameter)
Cone(diameter,height)
Cuboid(Lx,Ly,Lz)
Cylinder(diameter,height)
Ellipse(a,b)
Ellipsoid(a,b,c)
ImageShape(filename)
Layer(i)
Layers(i1,i2)
Rect(Lx,Ly)
Square(L)
Xrange(xmin,xmax)
Yrange(ymin,ymax)
Zrange(zmin,zmax)

Shape methods

Transl(dx,dy,dz)
Scale(sx,sy,sz)
RotX(angle)
RotY(angle)
RotZ(angle)
Repeat(dx,dy,dz)

Add(shape)
Sub(shape)
Inverse()
Intersect(shape)
Xor(shape)

```
// Rotated cheese example
```

```
d := 200e-9  
sq := square(d)  
  
h := 50e-9  
hole := cylinder(h, h)  
hole1 := hole.transl(100e-9, 0, 0)  
hole2 := hole.transl(0, -50e-9, 0)  
  
cheese := sq.sub(hole1).sub(hole2)  
cheese = cheese.rotz(pi/6)
```



rotated cheese

GEOMETRY

Optionally a magnet Shape other than the full simulation box can be specified

```
// Ring geometry example  
  
setGridsize(100, 100, 10)  
setCellsize(1e-9,1e-9,1e-9)  
  
ring := circle(100e-9).sub(circle(50e-9))  
  
setgeom(ring)  
  
save(geom)
```



REGIONS

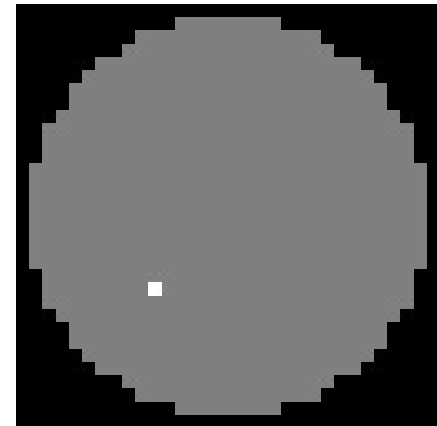
- 256 regions in total (index 0 → 255)
- Each cell is assigned to a single region (default region id is 0)
- Each region has its own set of material parameters
- Two ways to set the region id in cells:
 1. Set region id of a single cell
 2. Set region id of all cells in a shape

```
SetGridSize(32,32,1)
SetCellSize(1,1,1)

// Set region id of cells in a circle to 1
DefRegion(1, circle(30))

// Set region id of cell (10,10,0) to 2
DefRegionCell(2, 10, 10, 0)

Save(regions)
```



MATERIAL PARAMETERS

- Material parameters are assigned to the 256 regions.
- Material parameters can be functions of time
- There are vector and scalar material parameters
- Material parameters are predefined, they can not be created

```
// Assigning to a material parameter sets a value in all regions:  
Msat = 800e3  
AnisU = vector(1, 0, 0)  
  
// When regions are defined, they can also be set region-wise:  
Msat.SetRegion(0, 800e3)  
Msat.SetRegion(1, 540e3)  
  
// Material parameters can be functions of time as well:  
f := 500e6  
Ku1 = 500 * sin(2*pi*f*t)
```

MATERIAL PARAMETERS: EXCITATIONS

- An excitation is a regional material parameter
- Additionally, one can add an arbitrary number of time- and space-dependent vector fields of the form :

$$g(x_i, y_j, z_k) * f(t)$$

```
B_ext = vector(0,0,1)
```

```
B_ext.Add(LoadFile("antenna.ovf"), sin(2*pi*f*t))
```

```
B_ext.removeExtraTerms()
```

INITIAL MAGNETIZATION

Different ways to set the magnetization:

```
m = config  
m.LoadFile(filename)  
m.SetRegion(regionId, config)  
m.SetInShape(shape, config)  
m.SetCell(j,k,l, vector)
```

Here, a 'config' is an object which represents a magnetization configuration

INITIAL MAGNETIZATION

Config

Uniform(mx, my, mz)
RandomMag()
RandomMagSeed(seed)
TwoDomain(
 mx1, my1, mz1,
 my2, my2, mz2,
 mx3, my3, mz3)
Vortex(circ, pol)
AntiVortex(circ, pol)
VortexWall(mxLeft, mxRight, circ, pol)
NeelSkyrmion(charge, pol)
BlochSkyrmion(charge, pol)
Conical(kVec, coneDir, coneAngle)
Helical(kVec)

Config methods

Transl(dx,dy,dz)
Scale(sx,sy,sz)
Add(ratio, config)
RotZ(angle)

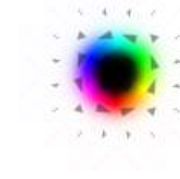
```
m = uniform(1,1,0)
```



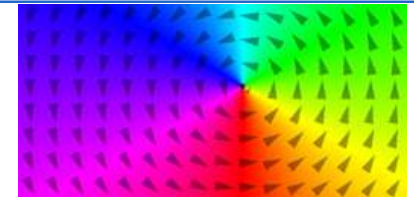
```
m=Vortex(1,-1).Add(0.1,randomMag())
```



```
M = BlochSkyrmion(1, 1)
```



```
m=Vortex(1,-1).transl(100e-9,50e-9,0)
```



```
m = uniform(1, 1, 1)  
m.setInShape(cylinder(400e-9,100e-9), vortex(1,-1))
```



OUTPUT

3 output media:

- log file for input, logging and printing
- table.txt (t, mx, my, mz, ...)

```
tableadd(E_total)
tableaddvar(myVar,"myVar","unit")
tablesave() // write single line
tableautosave(1e-12) // write periodically
```

- .ovf files for scalar and vector fields

```
save(Edens_total)
saveas(Edens_total,"edens.ovf")
autosave(Edens_total, 1e-10) // write periodically
```

RUN/RELAX/MINIMIZE

- Solving the LLG equation (time integration)

```
run(timeperiod)
steps(100)
runWhile(condition)
```

- Minimizing the energy

```
relax() // LLG without precession
Minimize() // steepest descent[1]
```

```
// WARNING: ADVANCED SETTINGS
// In most cases, these settings can be ignored

// Set the solver:
// 1:Euler, 2:Heun, 3:Bogaki-Shampine, 4: Runge-Kutta(RK45),
// 5:Dormand-Prince(the default), 6:Fehlberg, -1:Backward Euler
SetSolver(5)

// set timestep
fixdt = 0 // if 0 (default): use adaptive timestep

// Advanced settings for adaptive timestep (default values are given)
Headroom = 0.8 // headroom dt correction
MaxDt = 0 // if 0, no maximal timestep
MinDt = 0 // if 0, no minimal timestep
MaxErr = 1e-5 // maximum allowed error/step

// Advanced settings for minimizer (default values are given)
MinimizerSamples = 10 //Number of max dM for convergence check
MinimizerStop = 1e-6 //Stopping max dM for Minimize
```


THE INTERACTIONS

Effective field terms

- Demagnetization
- Exchange
- Anisotropy
- Dzyaloshinskii-Moriya
- External field
- Thermal field
- Custom field

Spin transfer torques

- Zhang-Li STT
- Slonczewski STT

DEMAGNETIZATION FIELD TERM

Demagnetization energy density

$$\varepsilon = -\frac{\mu_0}{2} M_s \mathbf{m} \cdot \mathbf{H}_{demag}$$

Regional Material Parameters	
Msat	Saturation magnetization (A/m)
NoDemagSpins	Disable magnetostatic interaction per region (default=0, set to 1 to disable).

Output Quantities	
B_demag	Magnetostatic field (T)
Edens_demag	Magnetostatic energy density (J/m3)
E_demag	Magnetostatic energy (J)

Other functionalities	
EnableDemag	Enables/disables demag (default=true)
SetPBC	Sets the number of repetitions in X,Y,Z to create periodic boundary conditions. The number of repetitions determines the cutoff range for the demagnetization.
DemagAccuracy	Controls accuracy of demag kernel

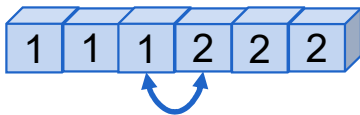
EXCHANGE FIELD TERM

Exchange energy density

$$\varepsilon = A (\nabla \mathbf{m})^2$$

Harmonic mean for inter-region exchange coupling (default behavior)

$$\frac{A}{M_s} = 2 \frac{\frac{A_1}{M_{s1}} \frac{A_2}{M_{s2}}}{\frac{A_1}{M_{s1}} + \frac{A_2}{M_{s2}}}$$



Regional Material Parameters

Aex	Exchange stiffness (J/m)
Msat	Saturation magnetization (A/m)

Output Quantities

B_exch	Exchange field (T)
Edens_exch	Total exchange energy density (including DMI) (J/m ³)
E_exch	Total exchange energy (including DMI) (J)
MaxAngle	Maximum angle between exchanged coupled spins (rad)

Other functionalities

Ext_InterExchange	Sets exchange coupling between two regions
Ext_ScaleExchange	Re-scales exchange coupling between two regions

ANISOTROPY FIELD TERM

Uniaxial anisotropy energy density

$$\varepsilon = -K_1 (\hat{u} \cdot \mathbf{m})^2 - K_2 (\hat{u} \cdot \mathbf{m})^4$$

Similar expression for cubic anisotropy energy density [1]

Regional Material Parameters

anisU	Uniaxial anisotropy direction
Ku1, Ku2	Uniaxial anisotropy constants (J/m ³)
AnisC1, AnisC2	Cubic anisotropy directions
Kc1, Kc2, Kc3	Cubic anisotropy constants (J/m ³)
Msat	Saturation magnetization (A/m)

Output Quantities

B_anis	Anisotropy field (T)
Edens_anis	Total anisotropy energy density (including DMI) (J/m ³)
E_anis	Total anisotropy energy (including DMI) (J)

DZYALOSHINSKII-MORIYA FIELD TERM

Interfacially-induced DMI energy density

$$\varepsilon = D [m_z(\nabla \cdot \mathbf{m}) - (\mathbf{m} \cdot \nabla)m_z]$$

Bulk DMI energy density

$$\varepsilon = D \mathbf{m} \cdot (\nabla \times \mathbf{m})$$

Note:

Only single DMI type allowed at once

Regional Material Parameters

Dind	Interfacially-induced DMI strength (J/m ²)
Dbulk	Bulk DMI strength (J/m ²)
Msat	Saturation magnetization (A/m)

Output Quantities

B_exch	Exchange field (including DMI) (T)
Edens_exch	Total exchange energy density (including DMI) (J/m ³)
E_exch	Total exchange energy (including DMI) (J)

Other functionalities

Ext_InterDind	Sets Dind coupling between two regions
Ext_ScaleDind	Re-scales Dind coupling between two regions
OpenBC	Use open boundary conditions (default=false, use Neumann BC). This setting is only relevant for DMI.

EXTERNAL FIELD TERM

Zeeman energy density

$$\varepsilon = -M_s \mathbf{m} \cdot \mathbf{B}_{ext}$$


Regional Material Parameters

Msat	Saturation magnetization (A/m)
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Excitation

B_ext	Externally applied field(T)
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Output Quantities

B_ext	Externally applied field(T)
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Edens_zeeman	Zeeman energy density (J/m ³)
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E_zeeman	Zeeman energy (J)
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THERMAL FIELD TERM

$$\langle \mathbf{H}_{th}(\mathbf{r}, t) \rangle = 0$$

$$\begin{aligned} \langle \mathbf{H}_{th}(\mathbf{r}, t), \mathbf{H}_{th}(\mathbf{r}', t') \rangle \\ = \frac{2k_B T \alpha}{M_s \gamma} \delta(\mathbf{r} - \mathbf{r}') \delta(t - t') \end{aligned}$$

Regional Material Parameters

Temp	Temperature (K)
alpha	Damping parameter
Msat	Saturation magnetization (A/m)

Output Quantities

B_therm	Thermal field (T)
Edens_therm	Thermal energy density (J/m ³)
E_therm	Thermal energy (J)

Other functionalities

ThermSeed	Sets random seed for thermal noise
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CUSTOM FIELD TERMS

Output Quantities	
B_custom	User-defined field (T)
Edens_custom	Total energy density of user-defined field (J/m ³)
E_custom	Total energy of user-defined field (J)

Other functionalities	
AddEdensTerm	Add a custom energy density term
AddFieldTerm	Add a custom effective field term
RemoveCustomFields	Remove all custom fields

ZHANG-LI STT

Zhang-Li spin-transfer torque

$$\boldsymbol{\tau} = \frac{1 + \xi\alpha}{1 + \alpha^2} \mathbf{m} \times (\mathbf{m} \times (\mathbf{u} \cdot \nabla) \mathbf{m}) + \frac{\xi - \alpha}{1 + \alpha^2} \mathbf{m} \times (\mathbf{u} \cdot \nabla) \mathbf{m}$$

with

$$\mathbf{u} = \frac{\mu_B P}{2e\gamma_0 M_s (1 + \xi^2)} \mathbf{j}$$

Regional Material Parameters	
Pol	Electrical current polarization
xi	Non-adiabaticity of spin-transfer-torque
alpha	Damping parameter
Msat	Saturation magnetization (A/m)
Excitation	
J	Electrical current density (A/m2)
Output Quantities	
STTorque	Spin-transfer torque/ γ_0 (T)
Other functionalities	
DisableZhangLiTorque	Disable Zhang-Li torque (default=false)

SLONCZEWSKI STT

Slonczewski spin-transfer torque

$$\boldsymbol{\tau} = \beta \frac{\epsilon + \alpha\epsilon'}{1 + \alpha^2} \mathbf{m} \times (\mathbf{m}_P \times \mathbf{m}) - \beta \frac{\epsilon' - \alpha\epsilon}{1 + \alpha^2} \mathbf{m} \times \mathbf{m}_P$$

with

$$\beta = \frac{j_z \hbar}{M_s e d} P \Lambda^2$$

$$\epsilon = \frac{P \Lambda^2}{(\Lambda^2 + 1) + (\Lambda^2 - 1)(\mathbf{m} \cdot \mathbf{m}_P)}$$

Regional Material Parameters

Pol	Electrical current polarization
Lambda	Slonczewski Λ parameter
EpsilonPrime	Slonczewski secondary STT term ϵ'
alpha	Damping parameter
Msat	Saturation magnetization (A/m)
FreeLayerThickness	Slonczewski free layer thickness (if set to zero (default), then the thickness will be deduced from the mesh size) (m)

Excitation

J	Electrical current density (A/m ²)
FixedLayer	Slonczewski fixed layer polarization

Output Quantities

STTorque	Spin-transfer torque/ γ_0 (T)
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Other functionalities

DisableSlonczewskiTorque	Disables Slonczewski torque (default=false)
FixedLayerPosition	Position of the fixed layer: FIXEDLAYER_TOP, FIXEDLAYER_BOTTOM (default=FIXEDLAYER_TOP)

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